

## fischer-inv<sup>11,40</sup>

$$\begin{aligned}
& \text{fischer-inv}\{i:l, \\
& \quad \$x:ut2, \\
& \quad \$try:ut2, \\
& \quad \$taken:ut2, \\
& \quad \$contending:ut2, \\
& \quad \$free:ut2, \\
& \quad \$mine:ut2, \\
& \quad \$wanted:ut2, \\
& \quad \$z:ut2\} \\
& \quad (es; L; del; e) \\
\equiv_{\text{def}} & ((\text{es-after}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$mine:ut2\}) \\
& \Rightarrow (l.\text{all}(L; \\
& \quad \text{Id}; \\
& \quad j.((\neg(j = \text{loc}(e))) \\
& \quad \Rightarrow \exists e'@j.\text{f-event}\{\$x:ut2\} \\
& \quad \quad (es; L; e') \\
& \quad \quad \wedge (\text{f-round}\{i:l\} \\
& \quad \quad \quad (\text{mkid}\{\$x:ut2\}; \text{mkid}\{\$free:ut2\}; es; e') \\
& \quad \quad \quad = \\
& \quad \quad \quad \text{f-round}\{i:l\} \\
& \quad \quad \quad \quad (\text{mkid}\{\$x:ut2\}; \text{mkid}\{\$free:ut2\}; es; e)) \\
& \quad \quad \wedge (\text{es-after}(es; \text{mkid}\{\$x:ut2\}; e') = \text{mkid}\{\$taken:ut2\}) \\
& \quad \quad \wedge \text{alle-at}(es; \\
& \quad \quad \quad j; \\
& \quad \quad \quad e''.((\text{f-round}\{i:l\} \\
& \quad \quad \quad \quad (\text{mkid}\{\$x:ut2\}; \text{mkid}\{\$free:ut2\}; es; e'' \\
& \quad \quad \quad \quad \quad ) \leq \text{f-round}\{i:l\} \\
& \quad \quad \quad \quad \quad \quad (\text{mkid}\{\$x:ut2\}; \\
& \quad \quad \quad \quad \quad \quad \text{mkid}\{\$free:ut2\}; \\
& \quad \quad \quad \quad \quad \quad es; \\
& \quad \quad \quad \quad \quad \quad e')) \\
& \quad \quad \Rightarrow \text{es-le}(es; e''; e')))) \\
& \wedge (\forall e':\text{es-E}(es). \\
& \quad \text{f-event}\{\$x:ut2\} \\
& \quad \quad (es; L; e') \\
& \quad \Rightarrow (\text{f-round}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:ut2\}; \text{mkid}\{\$free:ut2\}; es; e') \leq \text{f-round}\{i:l\} \\
& \quad \quad \quad (\text{mkid}\{\$x:ut2\}; \\
& \quad \quad \quad \text{mkid}\{\$free:ut2\}; \\
& \quad \quad \quad es; \\
& \quad \quad \quad e)) \\
& \Rightarrow (\text{ql}((\text{es-time}(es; e') + del); \text{es-time}(es; e)) \vee (e' = e))))
\end{aligned}$$

$$\begin{aligned}
& \wedge (\text{f-newround}\{\$x:\text{ut}2, \$\text{free}:\text{ut}2, \$\text{mine}:\text{ut}2\} \\
& \quad (es; L; e) \\
& \Rightarrow (\forall e':\text{es-E}(es). \\
& \quad (\text{loc}(e') \in L) \\
& \quad \Rightarrow @e'(\text{mkid}\{\$x:\text{ut}2\} \rightarrow \text{mkid}\{\$\text{free}:\text{ut}2\}) \\
& \quad \Rightarrow (\neg(\text{loc}(e') = \text{loc}(e))) \\
& \quad \Rightarrow (\uparrow\text{es-isrcv}(es; e')) \\
& \quad \Rightarrow (\text{es-tag}(es; e') = \text{mkid}\{\$\text{free}:\text{ut}2\}) \\
& \quad \Rightarrow (\text{es-lnk}(es; e') = \langle \text{loc}(e), \text{loc}(e'), \text{mkid}\{\$z:\text{ut}2\} \rangle) \\
& \quad \Rightarrow (\text{es-sender}(es; e') = e) \\
& \quad \Rightarrow (\text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e')) \\
& \quad = \\
& \quad \text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e))) \\
& \wedge (@e(\text{mkid}\{\$x:\text{ut}2\} \rightarrow \text{mkid}\{\$\text{try}:\text{ut}2\}) \\
& \Rightarrow (\forall e':\text{es-E}(es). \\
& \quad (\neg(\text{loc}(e') = \text{loc}(e))) \\
& \quad \Rightarrow (\uparrow\text{es-isrcv}(es; e')) \\
& \quad \Rightarrow (\text{es-tag}(es; e') = \text{mkid}\{\$\text{wanted}:\text{ut}2\}) \\
& \quad \Rightarrow (\text{es-lnk}(es; e') = \langle \text{loc}(e), \text{loc}(e'), \text{mkid}\{\$z:\text{ut}2\} \rangle) \\
& \quad \Rightarrow (\text{es-sender}(es; e') = e) \\
& \quad \Rightarrow ((@e'(\text{mkid}\{\$x:\text{ut}2\} \rightarrow \text{mkid}\{\$\text{taken}:\text{ut}2\}) \\
& \quad \Rightarrow (\text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e')) \\
& \quad = \\
& \quad \text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e))) \\
& \wedge (@e'(\text{mkid}\{\$x:\text{ut}2\} \rightarrow \text{mkid}\{\$\text{contending}:\text{ut}2\}) \\
& \Rightarrow (\text{f-rank}\{i:l\} \\
& \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e')) \\
& \quad = \\
& \quad \text{inc-snd}(\text{f-rank}\{i:l\}(\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e)))))) \\
& \wedge (\forall e':\text{es-E}(es). \\
& \quad \text{f-event}\{\$x:\text{ut}2\} \\
& \quad (es; L; e') \\
& \Rightarrow (\text{f-rank}\{i:l\} \\
& \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e')) \\
& \quad = \\
& \quad \text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e)) \\
& \Rightarrow \text{qle}(\text{qdist}(\text{es-time}(es; e); \text{es-time}(es; e')); \text{del}))
\end{aligned}$$

*clarification:*

fischer-inv{i:l},

$$\begin{aligned}
& \text{\$x:ut2,} \\
& \text{\$try:ut2,} \\
& \text{\$taken:ut2,} \\
& \text{\$contending:ut2,} \\
& \text{\$free:ut2,} \\
& \text{\$mine:ut2,} \\
& \text{\$wanted:ut2,} \\
& \text{\$z:ut2} \\
& (es; L; del; e) \\
\equiv_{\text{def}} & ((es\text{-after}(es; \text{mkid}\{\text{\$x:ut2}\}; e) = \text{mkid}\{\text{\$mine:ut2}\} \in \text{Id}) \\
& \Rightarrow (1.\text{all}(L; \\
& \quad \text{Id;} \\
& \quad j.((\neg(j = \text{es-loc}(es; e) \in \text{Id})) \\
& \quad \Rightarrow \text{existse-at}(es; \\
& \quad \quad j; \\
& \quad \quad e'.(\text{f-event}\{\text{\$x:ut2}\} \\
& \quad \quad \quad (es; L; e') \\
& \quad \quad \wedge (\text{f-round}\{i:l\} \\
& \quad \quad \quad (\text{mkid}\{\text{\$x:ut2}\}; \text{mkid}\{\text{\$free:ut2}\}; es; e') \\
& \quad \quad = \\
& \quad \quad \text{f-round}\{i:l\} \\
& \quad \quad \quad (\text{mkid}\{\text{\$x:ut2}\}; \text{mkid}\{\text{\$free:ut2}\}; es; e) \\
& \quad \quad \in \mathbb{N}) \\
& \quad \wedge (\text{es-after}(es; \text{mkid}\{\text{\$x:ut2}\}; e') = \text{mkid}\{\text{\$taken:ut2}\} \in \text{Id}) \\
& \quad \wedge \text{alle-at}(es; \\
& \quad \quad j; \\
& \quad \quad e''.((\text{f-round}\{i:l\} \\
& \quad \quad \quad (\text{mkid}\{\text{\$x:ut2}\}; \\
& \quad \quad \quad \text{mkid}\{\text{\$free:ut2}\}; \\
& \quad \quad \quad es; \\
& \quad \quad \quad e'' \leq \text{f-round}\{i:l\} \\
& \quad \quad \quad \quad (\text{mkid}\{\text{\$x:ut2}\}; \\
& \quad \quad \quad \quad \text{mkid}\{\text{\$free:ut2}\}; \\
& \quad \quad \quad \quad es; \\
& \quad \quad \quad \quad e')) \\
& \quad \Rightarrow \text{es-le}(es; e''; e'))))))) \\
& \wedge (\forall e':\text{es-E}(es). \\
& \quad \text{f-event}\{\text{\$x:ut2}\} \\
& \quad \quad (es; L; e') \\
& \quad \Rightarrow (\text{f-round}\{i:l\} \\
& \quad \quad (\text{mkid}\{\text{\$x:ut2}\}; \text{mkid}\{\text{\$free:ut2}\}; es; e') \leq \text{f-round}\{i:l\} \\
& \quad \quad \quad (\text{mkid}\{\text{\$x:ut2}\}; \\
& \quad \quad \quad \text{mkid}\{\text{\$free:ut2}\}; \\
& \quad \quad \quad es; \\
& \quad \quad \quad e)) \\
& \Rightarrow (\text{ql}(\text{es-time}(es; e') + del; \text{es-time}(es; e)) \vee (e' = e \in \text{es-E}(es))))))
\end{aligned}$$

$$\begin{aligned}
& \wedge (\text{f-newround}\{\$x:\text{ut}2, \$\text{free}:\text{ut}2, \$\text{mine}:\text{ut}2\} \\
& \quad (es; L; e) \\
& \Rightarrow (\forall e': \text{es-E}(es). \\
& \quad (\text{es-loc}(es; e') \in L \in \text{Id}) \\
& \quad \Rightarrow \text{es-change-to}(es; \text{Id}; \text{mkid}\{\$x:\text{ut}2\}; e'; \text{mkid}\{\$\text{free}:\text{ut}2\}) \\
& \quad \Rightarrow (\neg(\text{es-loc}(es; e') = \text{es-loc}(es; e) \in \text{Id})) \\
& \quad \Rightarrow (\uparrow \text{es-isrcv}(es; e')) \\
& \quad \Rightarrow (\text{es-tag}(es; e') = \text{mkid}\{\$\text{free}:\text{ut}2\} \in \text{Id}) \\
& \quad \Rightarrow (\text{es-lnk}(es; e') = \langle \text{es-loc}(es; e), \text{es-loc}(es; e'), \text{mkid}\{\$z:\text{ut}2\} \rangle \in \text{IdLnk}) \\
& \quad \Rightarrow (\text{es-sender}(es; e') = e \in \text{es-E}(es)) \\
& \quad \Rightarrow (\text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e')) \\
& \quad = \\
& \quad \text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e) \\
& \quad \quad \in (: \mathbb{N} \times \mathbb{N}))))) \\
& \wedge (\text{es-change-to}(es; \text{Id}; \text{mkid}\{\$x:\text{ut}2\}; e; \text{mkid}\{\$\text{try}:\text{ut}2\}) \\
& \Rightarrow (\forall e': \text{es-E}(es). \\
& \quad (\neg(\text{es-loc}(es; e') = \text{es-loc}(es; e) \in \text{Id})) \\
& \quad \Rightarrow (\uparrow \text{es-isrcv}(es; e')) \\
& \quad \Rightarrow (\text{es-tag}(es; e') = \text{mkid}\{\$\text{wanted}:\text{ut}2\} \in \text{Id}) \\
& \quad \Rightarrow (\text{es-lnk}(es; e') = \langle \text{es-loc}(es; e), \text{es-loc}(es; e'), \text{mkid}\{\$z:\text{ut}2\} \rangle \in \text{IdLnk}) \\
& \quad \Rightarrow (\text{es-sender}(es; e') = e \in \text{es-E}(es)) \\
& \quad \Rightarrow ((\text{es-change-to}(es; \text{Id}; \text{mkid}\{\$x:\text{ut}2\}; e'; \text{mkid}\{\$\text{taken}:\text{ut}2\}) \\
& \quad \Rightarrow (\text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e')) \\
& \quad = \\
& \quad \text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e) \\
& \quad \quad \in (: \mathbb{N} \times \mathbb{N}))))) \\
& \wedge (\text{es-change-to}(es; \text{Id}; \text{mkid}\{\$x:\text{ut}2\}; e'; \text{mkid}\{\$\text{contending}:\text{ut}2\}) \\
& \Rightarrow (\text{f-rank}\{i:l\} \\
& \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e')) \\
& \quad = \\
& \quad \text{inc-snd}(\text{f-rank}\{i:l\}(\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e)) \\
& \quad \in (: \mathbb{N} \times \mathbb{N})))))) \\
& \wedge (\forall e': \text{es-E}(es). \\
& \quad \text{f-event}\{\$x:\text{ut}2\} \\
& \quad (es; L; e') \\
& \Rightarrow (\text{f-rank}\{i:l\} \\
& \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e')) \\
& \quad = \\
& \quad \text{f-rank}\{i:l\} \\
& \quad \quad (\text{mkid}\{\$x:\text{ut}2\}; \text{mkid}\{\$\text{free}:\text{ut}2\}; es; e) \\
& \quad \quad \in (: \mathbb{N} \times \mathbb{N})) \\
& \Rightarrow \text{qle}(\text{qdist}(\text{es-time}(es; e); \text{es-time}(es; e')); \text{del}))
\end{aligned}$$

